

## Article

# Design Parameters of Vortex Pumps: A Meta-Analysis of Experimental Studies

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**Abstract:** Vortex pumps can impel solid-containing fluids and are therefore widely applied, from wastewater transport to the food industry. Despite constant efforts to improve vortex pumps, however, they have remained relatively inefficient compared to conventional centrifugal pumps. To find an optimized design of vortex pumps, this paper provides a systematic analysis on experimental studies that investigated how variations in geometric parameters influence vortex pump characteristics, in particular the pump head, the pressure coefficient and the efficiency for best point operation. To this end, an extensive literature search was conducted, and eighteen articles with 53 primary investigations were identified and meta-integrated. This showed that it is not yet clarified how vortex pumps operate. Two different assumptions of the underlying operating principle of a vortex pump lead to diverging design principles. From the results of this meta-analysis, we deduce recommendations for a more efficient design of a vortex pump and emphasize further aspects on the underlying operating principle of a vortex pump.

**Keywords:** vortex pump; recessed impeller; enlarged side chamber; meta-analysis; design parameters; operating principle; experimental studies

## 1. Introduction

The semi-open, recessed impeller and the enlarged side gap at the front chamber are the characteristics of vortex pumps that impel fluids with solid and fibrous material at a minimal risk of clogging. However, the efficiency of vortex pumps has remained relatively poor compared to conventional centrifugal pumps. In times of raising energy prices and strict energy goals that aim at slowing climate change, designing more efficient vortex pumps seems more desirable than ever. The aim of this paper is to find an improved design of vortex pumps in terms of efficiency and flow characteristics. To this end, an extensive literature search was conducted. Eighteen articles were identified and meta-integrated. All articles varied geometrical aspects in the impeller and/or the casing and then reported the pump characteristics. From these results, we deduce recommendations for a more efficient design. The literature search revealed that vortex pumps were designed according to two diverging design principles: the covered design or the open design. Both are based on different assumptions of the underlying operating principle of a vortex pump.

This review focuses on journal articles and conference articles that were publicly available at the time of the literature search. Eligible articles include single-parameter and/or multi-parameter experimental setups that measured how the geometry of the impeller and/or the geometry of the casing influenced the vortex pump characteristics (e.g., its head and efficiency). The results of computer-based simulations were excluded, but occasionally referred to if they contributed to a better comprehension

of the material presented. From spring 2015 until autumn 2015, we searched the databases of Google Scholar (<https://scholar.google.com>) for all articles containing the following keywords in the title or abstract: vortex pump, turo pump, recessed impeller, volute width, enlarged gap, side chamber gap, centrifugal pump. Because a large number of Chinese articles were found in the initial search, an additional search was conducted in spring 2015 using the database of the China Academic Journal Electronic Publishing House (<http://www.cnki.net>) and the corresponding Chinese keywords. All hits were scanned with respect to their validity and content. The final sample contained 18 articles with 53 primary investigations. All of the eligible articles presented single-parameter experiments that vary only one configuration at a time while holding all other configurations constant.

Figure 1 and Table 1 list all considered parameters in both the single-parameter and the multi-parameter experiments. Additionally, Table 1 identifies the articles that provided the empirical base for assessing these parameters. The geometric design parameters and the operation data of the Best Efficiency Point (BEP) were extracted from all articles. If the values were not explicitly mentioned, we estimated them from the respective graphs.

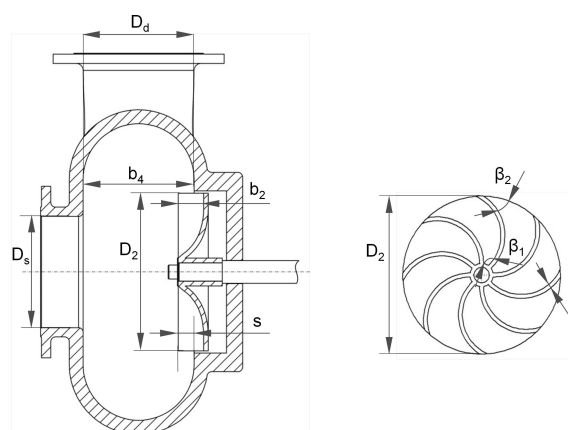


Figure 1. Considered parameters of a vortex pump.

Table 1. Assessed parameters in the articles.

Assessed Parameter	Prefix	Source(s)
Impeller width	$b_2$	Rütschi [1], Guan et al. [2] ([3]), Wang [4]-a, Wang [4]-b, Zheng et al. [5], Sha et al. [6], Sha et al. [7], Sha et al. [8], Ohba et al. [9], Masanori [10]
Impeller diameter	$D_2$	Rütschi [1], Guan et al. [2] ([3]), Wang [4]-c, Wang [4]-d, Zheng et al. [5], Sha et al. [6], Sha et al. [7], Sha et al. [8], Ohba et al. [9]-a, Ohba et al. [9]-b, Lubieniecki [11]-a, Lubieniecki [11]-b, Lubieniecki [11]-c
Blade number	$z$	Rütschi [1], Guan et al. [2] ([3]), Masanori [10],
Blade outlet angle	$\beta_2$	Guan et al. [2] ([3]), Sha et al. [6], Sha et al. [8], Masanori [10]
Blade inlet angle	$\beta_1$	Guan et al. [2] ([3])
Blade thickness	$t$	Guan et al. [2] ([3])
Winglets and front shroud	-	Zheng et al. [5], Jiang et al. [12] ([13]), Gerlach et al. [14]

Table 1. Cont.

	Assessed Parameter	Prefix	Source(s)
Casing	Volute width	b <sub>4</sub>	Zheng et al. [5] ([15]), Sha et al. [6], Sha et al. [7], Sha et al. [8], Ohba et al. [9]
	Covering	s	Rütschi [1]-a, Rütschi [1]-b, Sha and Hou [16]
	Suction pipe diameter	D <sub>s</sub>	Guan et al. [2] ([3]), Zheng et al. [5], Sha et al. [6], Ohba et al. [9]
	Geometry of suction inlet pipe	-	Rütschi [1]
	Pressure pipe diameter	D <sub>d</sub>	Zheng et al. [5]
	Geometry of casing	-	Zheng et al. [5]
	Rotation speed	n	Li and Feng [17]-a, Li and Feng [17]-b, Sha and Bai [18] ([19])

Note: Articles in parenthesis used the same experimental results as the aforementioned articles did.

Some authors investigated the influence of a parameter on slight different configurations of a vortex pump and published it in the same article. For example, the author Wang [4] investigated the influence of impeller width on an impeller with a diameter of 195 mm, but also tested the influence of impeller width on an impeller with a diameter of 180 mm. To distinguish between these two primary investigations of the same article for the same assessed parameter, we used the notation Wang [4]-a for the first primary investigation and Wang [4]-b for the second primary investigation (cp. second column of Table 1). Similar, it applies to studies of other authors (e.g., for the impeller diameter as assessed parameter: Wang [4]-c and Wang [4]-d ; Ohba et al. [9]-a and Ohba et al. [9]-b; Lubieniecki [11]-a, Lubieniecki [11]-b and Lubieniecki [11]-c). Therefore, Table A1 of the Appendix summarizes the geometry data of the 53 primary investigations.

Several studies were not integrated into this review because of their internal scaling (e.g., [20–22]), missing data (e.g., [15]), ambiguous representation of the data (e.g., parts of [2]), non-experimental nature and/or missing validation of the simulations (e.g., [23–29]). Some primary studies varied more than one parameter at a time when reporting the characteristics ([1,2,4,9,11,17] and [8] (similar in [30])). However, the primary studies were limited to single-parameter investigations because it is the only setup that allows isolating how distinct variations affect the BEPs. Further, deductions can be hardly derived from the multi-parameter investigations due to missing data and missing parameter variations.

## 2. Design Principles of Vortex Pumps

The literature search revealed that vortex pumps were designed according to one of two design principles: the covered design or the open design.

### 2.1. Covered Design

In the covered design (Figure 2a), the impeller is set back into the casing, and the casing thus completely covers the radial impeller outlet (as Figure 2b illustrates). Researchers who follow this design concept likely assume that the operating principle of vortex pumps is comparable to a hydraulic coupling, where the impeller induces a vortex in the enlarged side chamber and thereby transports the fluid (e.g., [11,29]). Given that this operating principle is at work, it seems most beneficial to cover the impeller to the casing. Doing so allows the forming of stronger vortices in the front chamber. Hence, the working transmission of the impeller would release its force to the fluid on the front side, and only small losses occur at the radial exit of the impeller. The literature search yielded that at least 32 out of 53 articles used the covered design, while the exact design was unspecified in 13 articles.

The covered design is sometimes associated with pan impellers whose shape is either rectangular (Figure 3a) or round (Figure 3b). Both impellers were likely designed with the intent to optimize the vortex formation. The geometric closing of both impellers' radial outlet creates an axial energy transfer to the side chamber. In this case, the round shape (Figure 3b) seems the more suitable form because the round shape guarantees a better guidance of the fluid flow. Overall, it is noteworthy that a pan impeller is not a necessity for the covered designs, although eight out of the 32 investigations on covered designs used them ([9,10]).

Various authors developed fluid transport models for the covered designs and pan impellers. For example, Schivley and Dussourd [20], Aoki ([31,32]) and Ohba and colleagues ([9,22,33]) developed predicting methods for the performance and design methods for vortex pump impellers.



**Figure 2.** (a) Vortex pump according to the covered design; and (b) schematic illustration of the covered design.

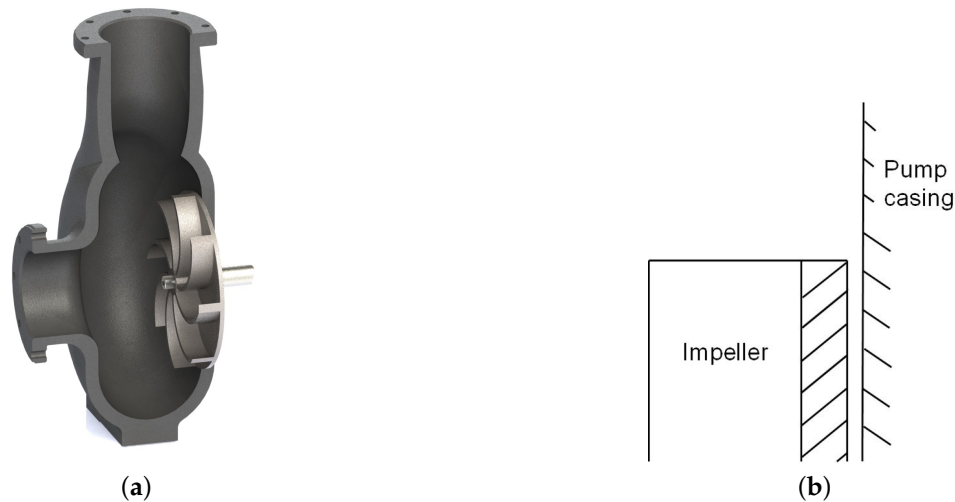


**Figure 3.** Examples of pan impellers. (a) Rectangular shape; and (b) rounded shape.

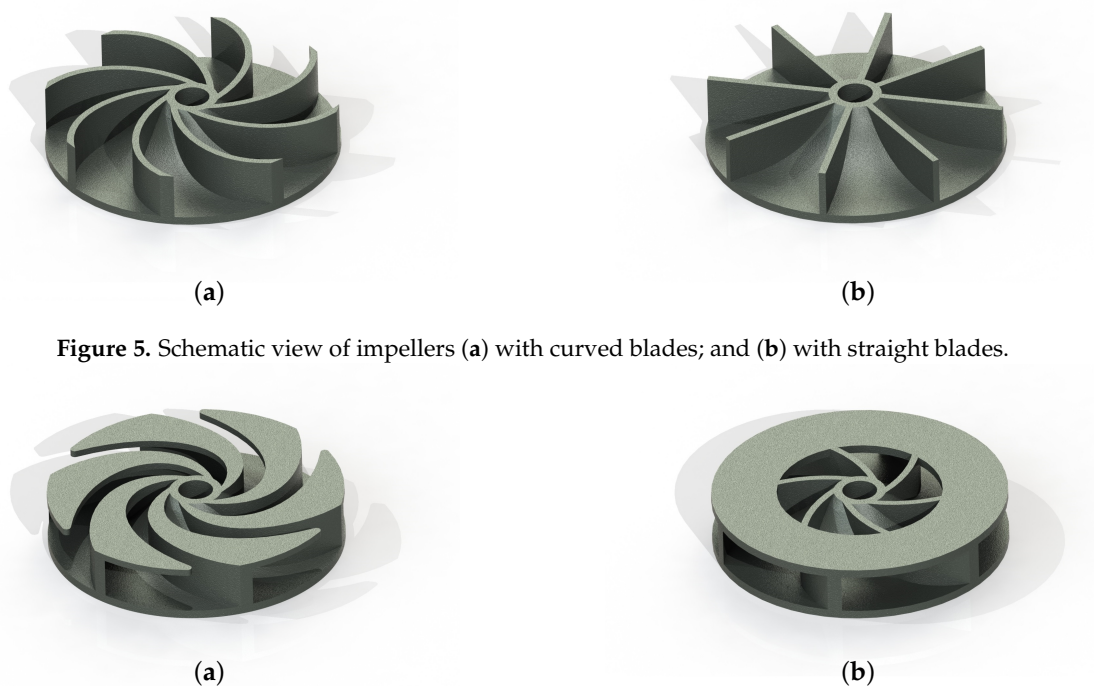
## 2.2. Open Design

An alternative design principle of vortex pumps is the open design. Here, the casing does not cover the impeller. Instead, the vortex pump looks similar to a centrifugal pump with a semi-open impeller and wide front gap (Figure 4a,b). The assumed operating principle is that of a conventional centrifugal pump: fluids are transported through the impeller itself and without the assistance of a vortex. Due to the wide front gap, however, exchange losses occur. These losses would explain the relatively low efficiency and the relatively low head of vortex pumps compared to conventional centrifugal pumps (e.g., [1]). Given that the working principles of vortex pumps and conventional pumps are similar, it follows that comparable design recommendations apply to vortex pumps as they do to conventional centrifugal pumps. For example, an impeller overlapping with the casing would disrupt the outflow from the impeller and, hence, increase losses.

In the open design, the impeller frequently resembles a semi-open impeller, similar to that of a conventional centrifugal pump. The blades are curved or straight and, in both cases, pulled up to the hub (Figure 5a,b). This design can be modified when winglets are added to the front edges of the blades. Figure 6a is an example of an impeller with winglets. The maximal execution on winglets results in a front shroud (Figure 6b).



**Figure 4.** (a) Vortex pump according to the open design; and (b) schematic illustration of the open design.



**Figure 5.** Schematic view of impellers (a) with curved blades; and (b) with straight blades.



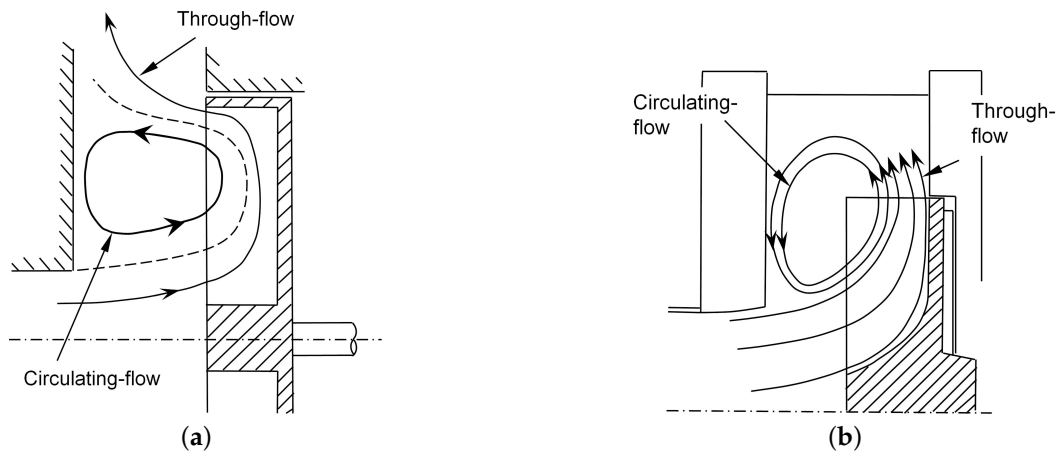
**Figure 6.** Schematic view of impellers (a) with winglets; and (b) with front shroud.

### 2.3. Interim Conclusion

Overall, the covered design and the open design are based on different assumptions about the underlying operating principle of a vortex pump. Because it is unclear which of the two operating principles is mainly responsible for the fluid transport, it is unknown which of the two design

types should be prioritized in the first place (in terms of higher head and greater efficiencies). As a consequence, it is unclear which geometric modifications ultimately optimize vortex pumps.

Regardless of the operating principles at work, the fluid flow in the front chamber can be principally divided into two components: a through-flow and a recirculating flow. Figure 7a,b illustrates the two flows on behalf of the covered design (Figure 7a) and the open design (Figure 7b), respectively. It is an open question to what degree each component contributes to the fluid transport and to what degree the two components can be separated.



**Figure 7.** (a) Flow model for the covered design (adapted from [31]); and (b) flow model for the open design (adapted form [34]).

### 3. Results

#### 3.1. Presentation of Data

For the presentation of the data, we used the values head ( $H$ ) or correspondingly the dimensionless value pressure coefficient ( $\psi$ ) and the efficiency ( $\eta$ ). The pressure coefficient is a dimensionless quantity that can be derived from the model laws and serves to characterize the operating behavior of a pump. It describes the head of a pump. The pressure coefficient is defined as:

$$\psi = \frac{2 \cdot g \cdot H}{\pi^2 \cdot n^2 \cdot D_2^2} \quad (1)$$

with the gravitational acceleration  $g$ , the head  $H$ , the rotation speed  $n$  and the impeller diameter  $D_2$ .

The efficiency is a ratio to characterize the quality of a machine. It sets the effective power in relation to the consumed power. For pumps, different efficiencies can be named, as for example the hydraulic efficiency or the aggregate efficiency, depending on which power serves as effective power or consumed power. In this study, we did not distinguish between authors using hydraulic efficiencies or aggregate efficiency, as none of the considered articles provided any information, and it was sufficient to determine trends.

Figure 8 illustrates how the head curves, pressure coefficient curves and the efficiency curves from the primary studies were generated (on the left). The example shows how variations in the impeller width affected the head ( $H$ ) and the pressure coefficient ( $\psi$ ; both at the top right panel) and efficiency ( $\eta$ ; at the bottom right panel). When integrating primary studies, first the highest efficiency for each impeller width was read off and thereby defining its operation point for best efficiency ( $BEP$ ). All  $BEP$ s were combined into a single graph by plotting them against their respective impeller width. Finally, a linear trend line was fitted through all  $BEP$ s of each primary study. These steps were repeated for all primary studies. This representation allows displaying multiple studies in a single graph at the cost of reducing the analyses to comparing  $BEP$  values.



To distinguish between the *BEPs* from different design principles of vortex pumps (e.g., covered design, open design), the following coding scheme is used for all symbol markers in the figures: grey- or black-filled markers represent covered designs of vortex pumps with semi-open impellers (e.g., [8] in Figure 8); cross markers represent covered designs of vortex pumps with pan impellers, either square-shaped or round-shaped impellers (e.g., [10] in Figure 8); black/white two-faced markers represent the open designs of vortex pumps; non-filled markers represent non-specified designs with unknown impeller types (e.g., [5] in Figure 8).

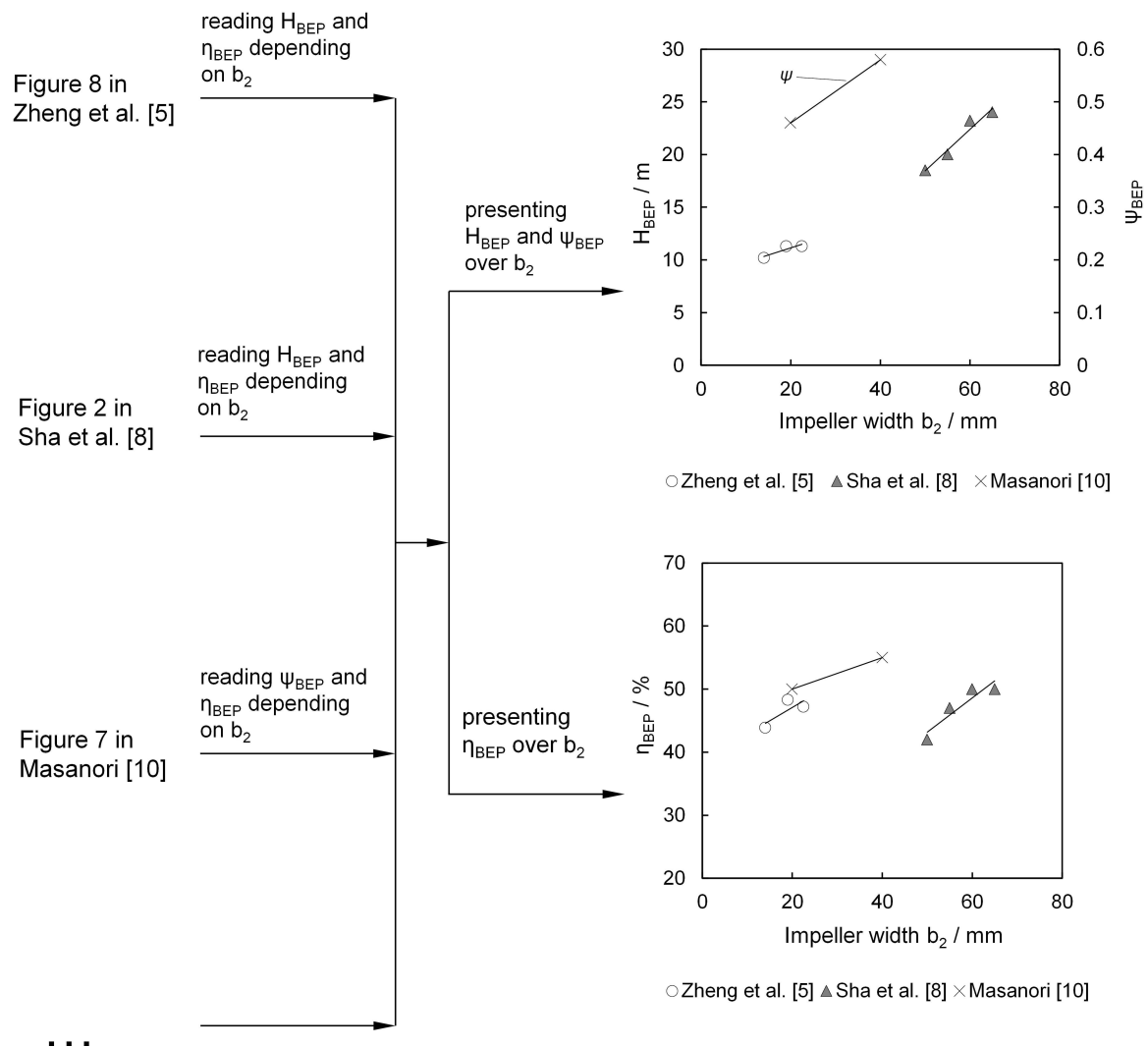


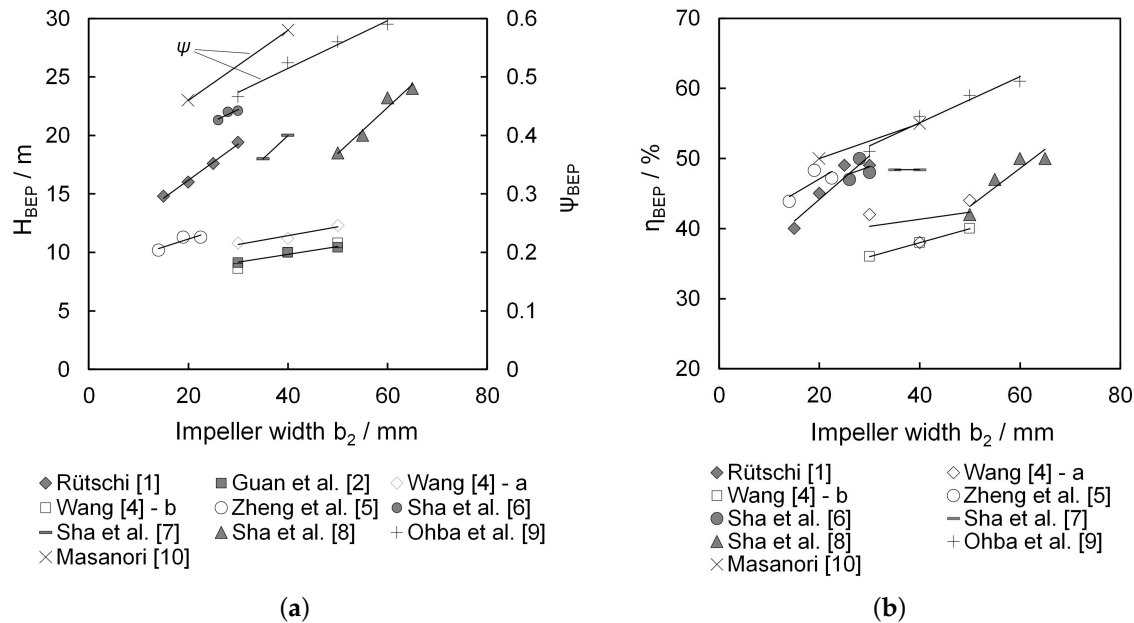
Figure 8. Example for the presentation of the data.

### 3.2. Single-Parameter Investigations

#### 3.2.1. Impeller Width

The impeller width refers to the depth of the blades. Figure 9a pictures the head and the pressure coefficient over the impeller width. Figure 9b shows the efficiency at the *BEP* for each vortex pumps. Generally speaking, the results suggest that a larger impeller width leads to greater head and higher pressure coefficients. The relation between the impeller width and efficiency is not as clear. Whereas the majority of the studies suggest the efficiency increases with the impeller width increasing, some studies [5,6] suggest a threshold for this trend after which the efficiency drops.

Figure 9a,b shows that the gradients of trend lines differ between the studies. This suggests the presence of the confounding influences of other design parameters. The studies differed in their vortex pump design principle, but also in their specific design, for example the casing design, the volute width, blade number, etc. That might influence the maximum reached head and efficiency, as well, and leads to different trends and absolute values between the studies.



**Figure 9.** (a) Head and pressure coefficient over impeller width; and (b) efficiency over impeller width.

### 3.2.2. Impeller Diameter

The majority of the primary studies assessed the effect of varying the impeller diameter. Overall, these studies univocally conclude that increasing the impeller diameter yields greater head and pressure coefficients. This is in accordance with insights from common centrifugal pumps where similar effects are known (e.g., [35,36]). Figure 10a plots the head for the *BEP* against the impeller diameter. Figure 10b plots the pressure coefficient for the *BEP* against the impeller diameter. Notably, the gradients between the studies differ substantially, suggesting the presence of confounding influences on the head characteristics. Here again, the studies differed in their specific design of tested vortex pump, leading probably to different trends and absolute values between the studies.

Figure 11 combines the studies of Figure 10a,b and plots the efficiency for the *BEP* over the impeller diameter. Overall, the trends suggest that greater impeller diameters lead to greater efficiency. However, this trend is not necessarily linear. The studies of Guan et al. [2], Zheng et al. [5] and Sha et al. [8] for example suggest a U-shaped relationship.



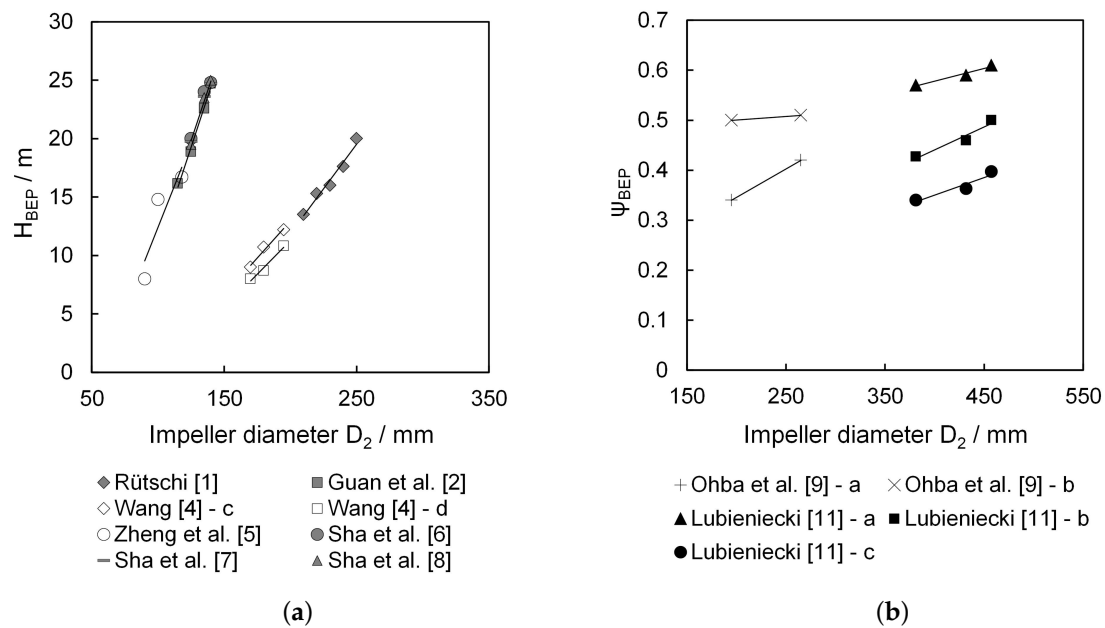


Figure 10. (a) Head over impeller diameter; and (b) pressure coefficient over impeller diameter.

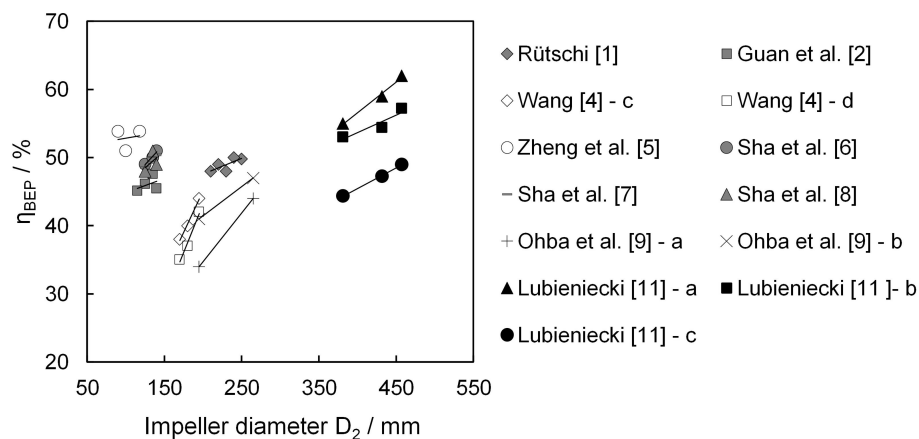
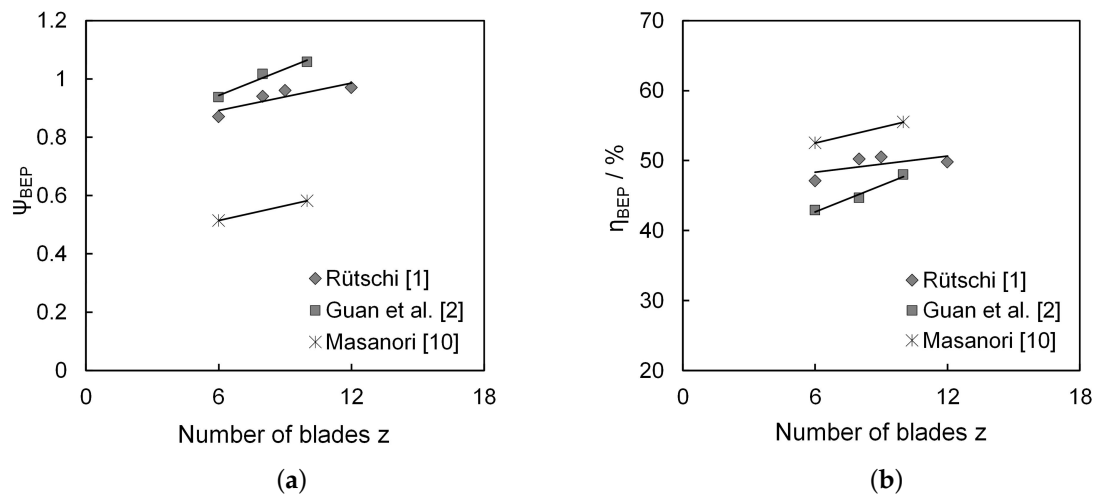


Figure 11. Efficiency over impeller diameter.

### 3.2.3. Number of Blades

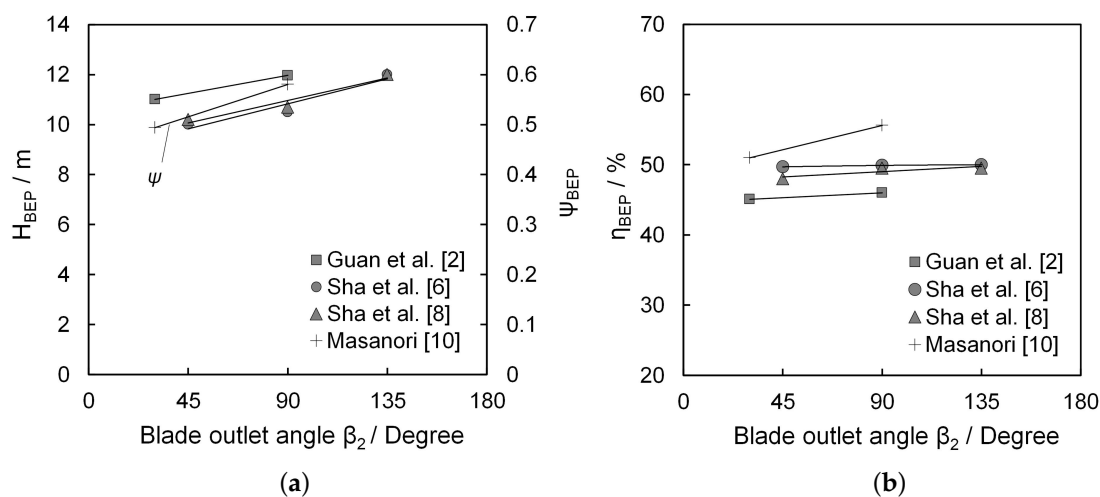
All studies suggest that an increased blade number leads to greater pressure coefficients and greater efficiency. Figure 12a shows the influence of the number of blades on the pressure coefficient for the *BEP*. Figure 12b plots blade numbers against efficiency. Noteworthy, Rüttschi [1] reported a decreasing efficiency for 12 blades. In combination with the other studies, this suggests that more than 10 blades are not beneficial.



**Figure 12.** (a) Pressure coefficient over number of blades; and (b) efficiency over number of blades.

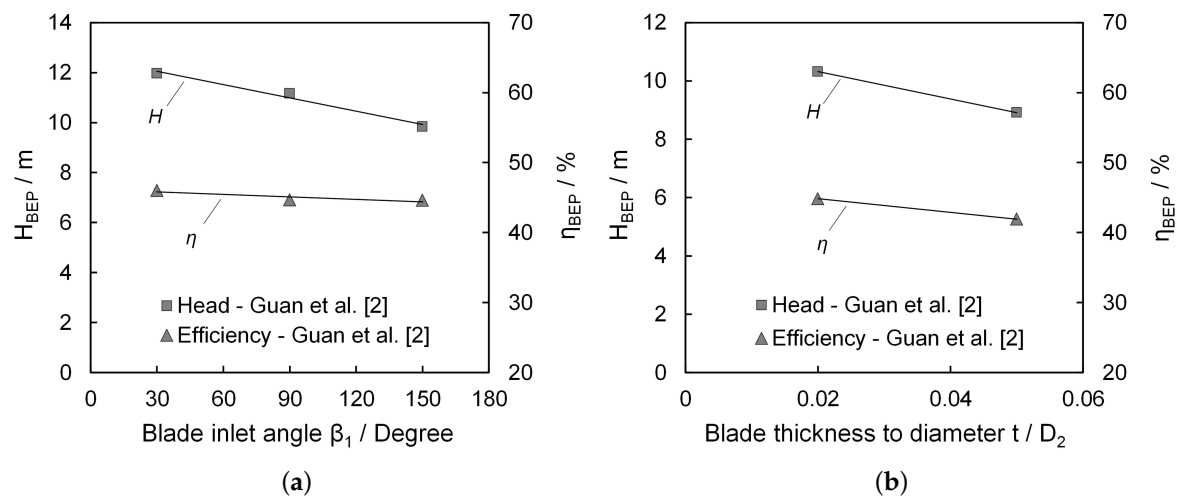
### 3.3. Blade Angles

The influence of the blade angle was studied in two ways: either by changing the blade outlet angle  $\beta_2$  at a constant blade inlet angle  $\beta_1$  or, vice versa, by changing the blade inlet angle  $\beta_1$  at a constant outlet angle  $\beta_2$ . Overall, increasing the outlet angle seems to increase the head and the pressure coefficient. Greater angles thus lead to more efficiency. In contrast, the transition from straight blades to forward curved blades is marginal. Figure 13a summarizes the influence of the blade outlet angle  $\beta_2$  on the pressure coefficient. The results suggest that increasing the blade outlet angle improves the pressure coefficient. In particular, it is demonstrated that an impeller with an outlet angle greater than  $90^\circ$  (i.e., forward curved blades) is associated with greater pressure coefficients. Figure 13b plots the influence of the blade outlet angle  $\beta_2$  against efficiency. This shows the tendency of increasing efficiency with increasing blade angle.



**Figure 13.** (a) Head and pressure coefficient over blade outlet angle; and (b) efficiency over blade outlet angle.

Guan et al. [2] examined the influence of varying the blade inlet angle  $\beta_1$ . Figure 14a shows the results for head and efficiency that suggest increasing the inlet angle decreases the head and slightly the efficiency.



**Figure 14.** (a) Head and efficiency over blade inlet angle; and (b) head and efficiency over blade thickness to impeller diameter.

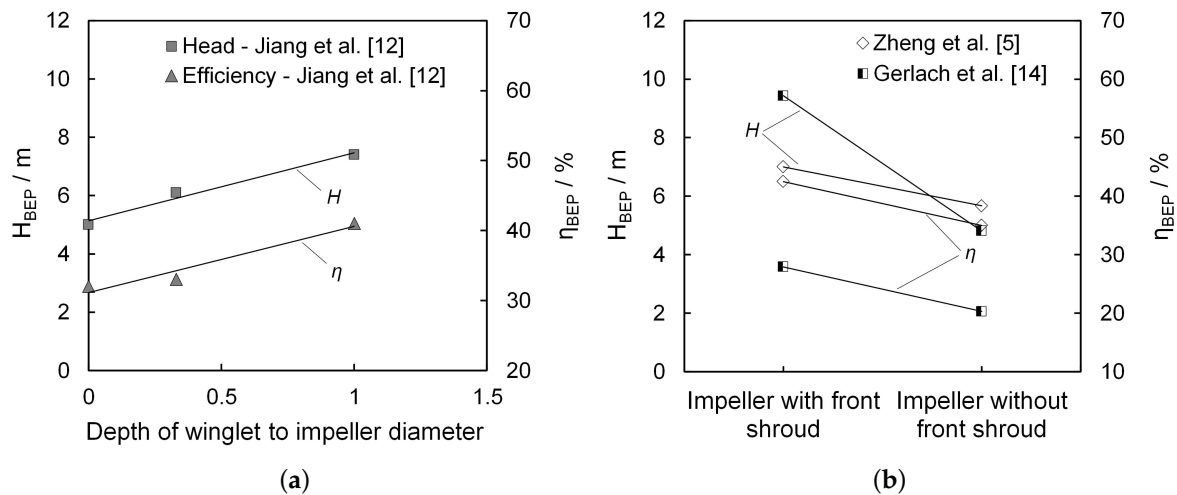
### 3.4. Blade Thickness

Only a single study examined the influence of varying the blade thickness [2]. Figure 14b suggests that the head and the efficiency of the *BEP* drop with blade thickness increasing. However, only two configurations were tested.

### 3.5. Winglets and Front Shrouds

Jiang et al. [12] examined the impact of adding winglets to a semi-open impeller. The study compared two different winglet depths to an impeller without winglets. Figure 15a shows the results for head and efficiency over the ratio of winglet depth to impeller diameter. Overall, the head and the efficiency of the impellers with winglets were lower than those of the impeller without winglets. Decreasing the ratio of winglet depth to impeller diameter was associated with a lower head and lower efficiency. Notably, another study by Gerlach et al. [14] demonstrated that adding winglets to a vortex pump with free outflow from the impeller (i.e., without coverage) and four curved blades led to a greater head and more efficiency. On a further note, Cervinka [24] investigated the operation of winglets using a numerical model. The author compared an impeller with winglets with a geometrically similar impeller without winglets. The study concluded that an impeller with winglets deteriorates the pump characteristic and its efficiency. These results have not been experimentally validated however, and they contradict the measurement results of Jian et al. [12] and Gerlach et al. [14].

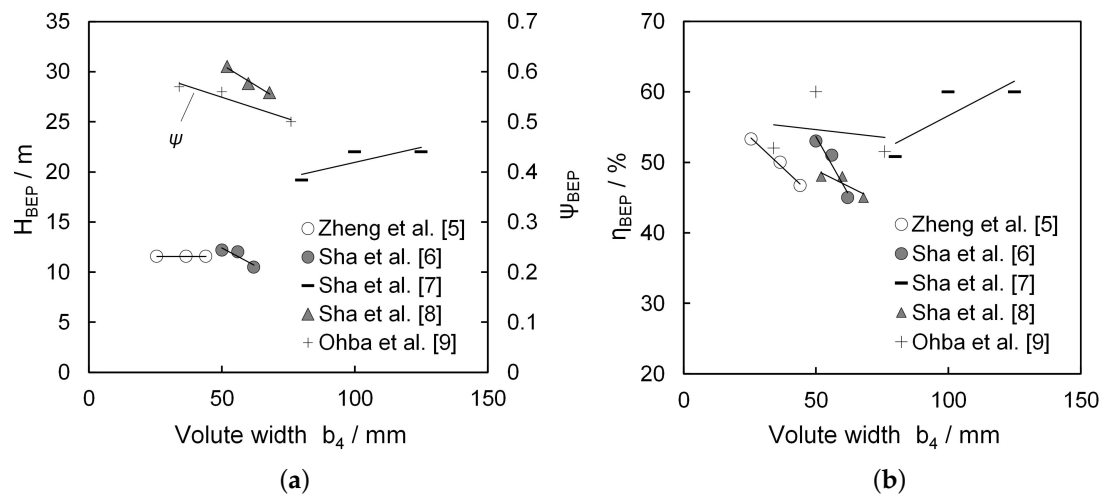
The maximal design of winglets results in a front shroud. Adding a front shroud strongly limits the use of vortex pumps (e.g., for pumping solid-containing fluids); however, such a modification can prove insightful for understanding the principle characteristics of a vortex pump. Figure 15b shows the results for an impeller without a front shroud compared to an impeller with a front shroud. Adding the front shroud was associated with a greater head and more efficiency compared to the semi-open impeller.



**Figure 15.** (a) Head and efficiency over depth of winglet; and (b) head and efficiency for impellers with and without a front shroud.

### 3.6. Volute Width

The volute width refers to the width of side chamber gap between the casing and the impeller. Figure 16a shows the head and pressure coefficient over the variation of volute width. All, but one study (Sha et al. [7]), suggested that the head and pressure coefficient decrease when the volute width increases. Figure 16b plots the associated efficiencies. Again, all but one study (Sha et al. [7]) suggested that the efficiency decreases when volute width increases. Each study seems to have its own optimal efficiency point depending on the volute width. A parabolic curve seems to fit the measurement points better than a linear trend line.



**Figure 16.** (a) Head and pressure coefficient over volute width; and (b) efficiency over volute width.

### 3.7. Covering of the Impeller

The covering of the impeller refers to the overlap between the impellers' radial outlet and the casing. Figure 17a depicts how decreasing the covering affects the head for the BEP. At zero, the impeller completely covers the casing. With increasing values, the covering decreases until the impeller is completely uncovered (the maximum value for each study; e.g., 20 mm in Rüttschi [1]). Figure 17a suggests that covering the impeller decreases the head. Figure 17b shows the associated efficiencies for the covering of the impeller. This suggests that covering the impeller decreases efficiency.

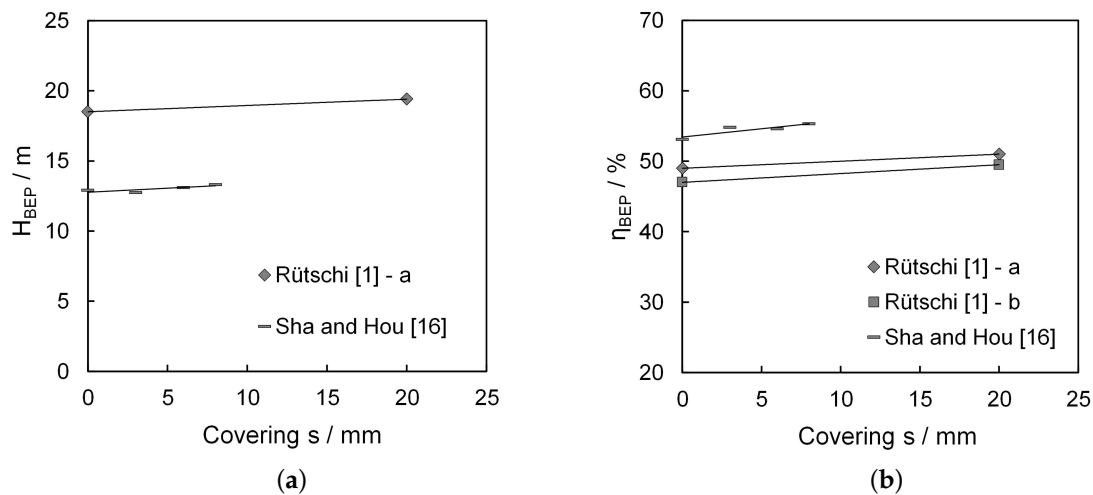


Figure 17. (a) Head over covering; and (b) efficiency over covering.

### 3.8. Suction Pipe Diameter

The suction pipe diameter refers to the pipe diameter at the suction entrance of the pump. Variations in the suction pipe diameter only marginally affect the head and the pressure coefficient. The effect of the suction pipe diameter on efficiency is contradictory. The studies of Sha et al. [6] and Ohba et al. [9] show an increase of efficiency with increasing suction pipe diameter, while the study of Zheng et al. [5] shows the opposite behavior. Only Guan et al. [2] shows no influence of suction pipe diameter on the efficiency. Figure 18a shows the results for the head and the pressure coefficient over the suction pipe diameter. Figure 18b shows the respective values for efficiency.

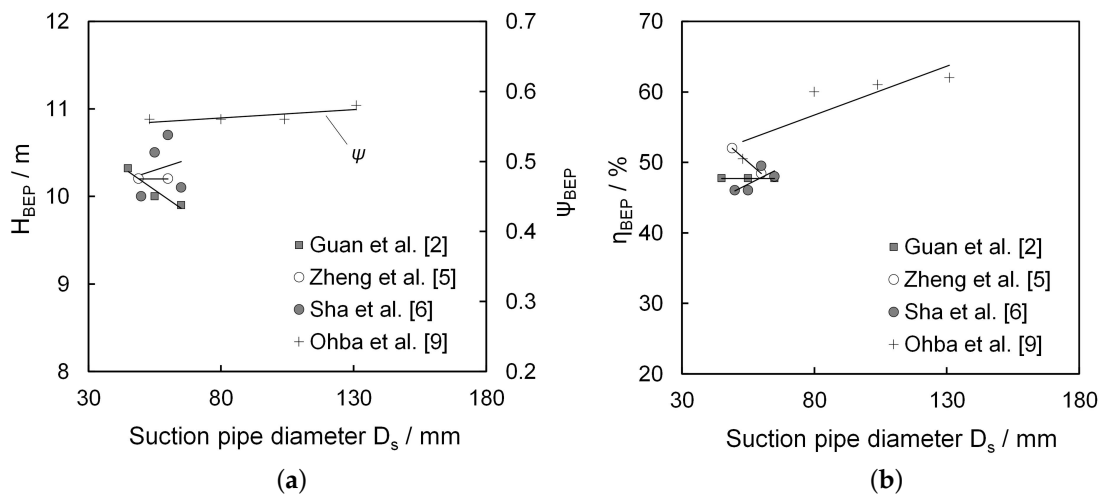
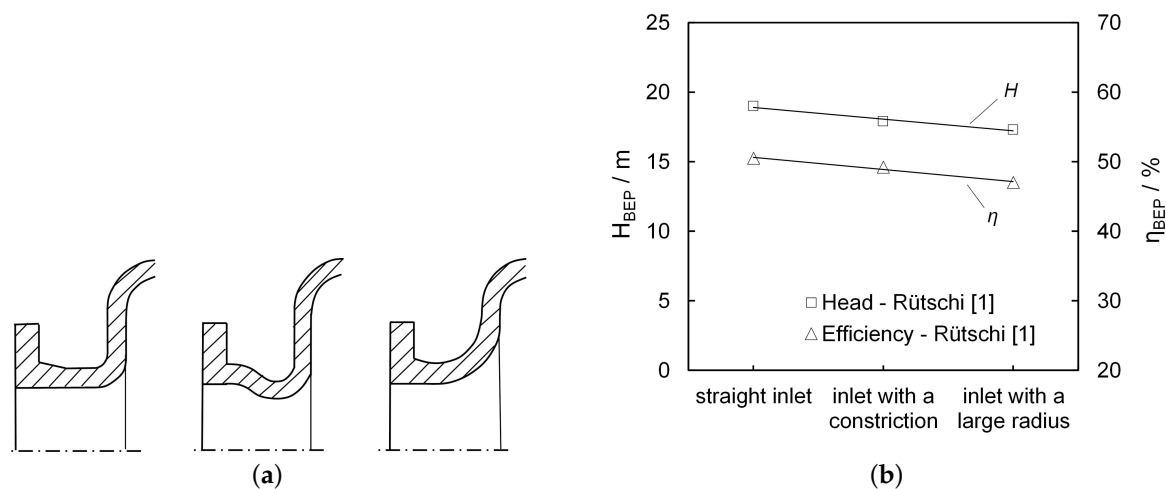


Figure 18. (a) Head and pressure coefficient over suction pipe diameter; and (b) efficiency over suction pipe diameter.

### 3.9. Suction Pipe Inlet Geometry

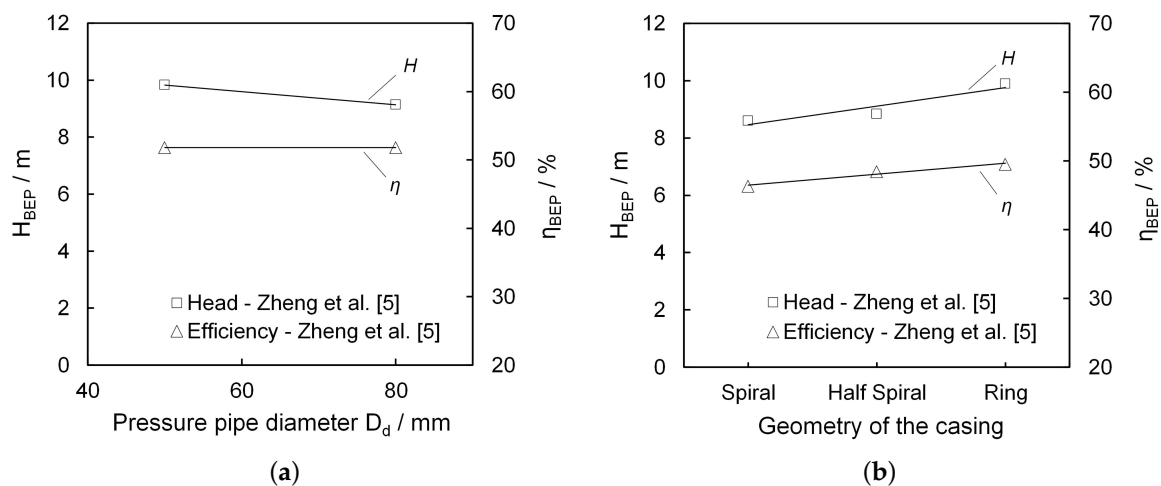
Only Rüttschi [1] examined the suction pipe inlet geometry, i.e., the design of inlet from the suction pipe of the pump to the casing. Three variations were considered, shown in Figure 19a (from left to right): a straight inlet, an inlet with a constriction and an inlet with a large radius of curvature. Figure 19b plots the results of the measurements against the head and efficiency. A straight inlet of the suction pipe seems preferable in terms of highest head and efficiency. The comparisons were based on an impeller with nine straight blades.



**Figure 19.** (a) Different inlet geometries of the suction pipes (based on [1]; from left): a straight inlet, an inlet with a constriction and an inlet with a large radius of curvature; and (b) influence of the suction pipe inlet geometry on the head and efficiency.

### 3.10. Pressure Pipe Diameter

A single study tested variations in the pressure pipe diameter by two configurations (Zheng et al. [5]). Figure 20a shows the associated head and efficiency. The results suggest that a large pressure pipe diameter decreases the head. The impact on the efficiency is insignificant. However, it has to be considered that only two configurations were tested, and correlations are hard to deduce.



**Figure 20.** (a) Head and efficiency over pressure pipe diameter; and (b) head and efficiency for different geometries of the casing.

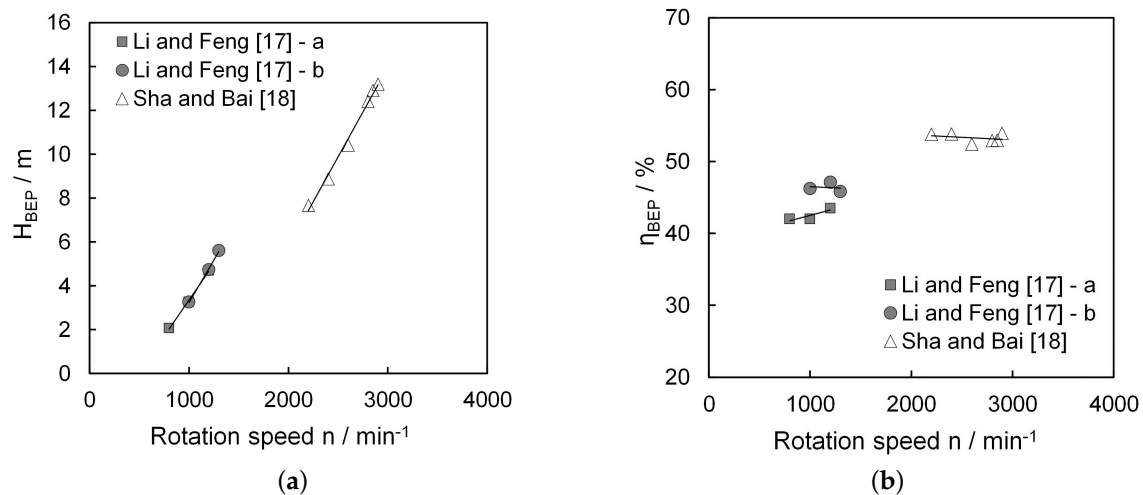
### 3.11. Geometry of the Casing

The geometry of the casing refers to the specific design of the casing, for example the comparison between a spiral casing or a ring casing. Figure 20b shows how the geometry of the casing influences the head and efficiency. The graph is based on the study of Zheng et al. [5]. The study compared a spiral casing with a ring casing and with a half spiral casing. Both head and efficiency were highest when the ring casing was used.



### 3.12. Rotation Speed

As depicted in Figure 21a, three studies univocally suggest that higher rotation speeds lead to greater head. In contrast, Figure 21b suggests that rotation speed has little effect on efficiency. The effect on head resembles insights on common centrifugal pumps for which similar effects have been observed (e.g., [35,36]).



**Figure 21.** (a) Head over rotation speed; and (b) efficiency over rotation speed.

### 3.13. Correlations between Parameters

Some of the single primary studies explicitly deduce recommendations about specific ratios for geometric parameters with the goal of maximizing head and/or achieving the highest efficiencies. Table 2 provides an overview on the recommended ratios. We tried to verify the suggested correlations based on all collected primary studies. For this propose, all studies were considered that indicated both parameters while testing one of them. For example, the relation between suction pipe diameter and impeller diameter, mentioned as 0.45 by Ohba et al. [22] (Table 2, last column), was tested by looking at all single primary studies that changed the suction pipe diameter with constant impeller diameter and vice versa. These studies were plotted over the ratio of suction pipe diameter to impeller diameter to identify optima. However, we failed to verify the suggested correlations. This was either because no studies tested the targeted correlations or the optimum itself did not exist.

**Table 2.** Recommended ratios for geometric parameters in articles.

Source	Relationship	Targeted Improvement	Conclusion
Rütschi [1]	$b_2/D_s = (0.25-0.30)$	Best efficiencies and head	Not confirmed
Ohba et al. [22]	$b_2/D_2 = 0.25$	Best efficiencies	Not confirmed
Ohba et al. [22]	$b_4/D_2 = 0.20$	Best efficiencies and head	Not confirmed
Zheng et al. [5]	$b_4/D_2 = 0.255$	Best efficiencies and head	Not confirmed
Ohba et al. [22]	$D_s/D_2 = 0.45$	Best efficiencies and head	Not confirmed

## 4. Discussion

As a major difference in the studies, the design type was highlighted, as explained at the beginning of this paper. This is to say, in some studies, a covered design was used, a pan impeller or less common a free flow impeller. However, it is assumed that this has a significant effect on the performance, since it possibly prevents the free flow out of the impeller. A study that compares the pan impeller with covering to a normal impeller with free outflow and without covering was partly shown by

Rütschi [1]. These tested impellers are not directly comparable due to many different parameters, so that a conclusion could not be drawn. However, testing such impellers, similar in parameters, but different by the type, would be the best way to face the assumed operating principles.

Some authors describe the optimal ratios of geometric parameters to each other to achieve the highest head and efficiencies. The described optima were considered on the basis of the collected data and could not be confirmed. However, it is important to note that the slopes of the suggested trends may considerably differ between the primary studies. These differences suggest that confounding, but unobserved factors exist that moderate the relations between the geometric variation and the observed behaviors. This suggests that trends for this type of pump might be described; however, a number of unknown factors exist, so definite and formula-based relationships are not yet grasped.

Despite the fact that volute width has been assessed in a number of studies, it often remains unclear how these measurements were exactly implemented. The volute width could be varied, for example, by varying the impeller widths or by moving the impeller in the casing, to change the distance between impeller and casing. Hence, the results should be interpreted with care. The same applies for the parameter covering. Here again, it is unclear how these experiments were implemented in detail and if a change in volute width took place. Therefore, the impact on the pump-specific performance is not entirely clear for this parameter, either.

Based on the data collected, it would be interesting to calculate characteristic values, such as the specific speed or the specific diameter. This might also possibly further hint at the operating principle of the pump. However, this was not possible because many of the studies did not fully publish the geometry data and/or operating data or scaled them internally. Thus, no comparability was possible. The fact to be scrutinized is that in some cases, the same measurements were found in various publications.

Overall, it is surprising that no literature works were found for the clogging behavior. Therefore, the results on the influence of the parameters always relate purely to the hydraulic data of the delivery and do not indicate the clogging behavior. This opens up a large field of research since vortex pumps are actually used for the transport of fluids with solids. The same applies for the usage of back vanes on vortex pumps. It is the practice of pump suppliers to use back vanes on vortex pump impellers, but no studies were found on that. Since it is known from classical centrifugal pumps that semi-open impellers increase the axial thrust, it is not reprehensible to adopt this to vortex pumps and apply back vanes as a countermeasure. However, this needs further clarification, since back vanes might influence the clogging behavior.

## 5. Conclusions

### 5.1. Influence of Parameters

We reviewed 53 primary studies that geometrically varied the characteristics of vortex pumps and measured their effect on the head, the pressure coefficient and efficiency for *BEP*. Table 3 summarizes these effects for geometric changes to the impeller. Table 4 summarizes these effects for geometric changes to the casing and to the rotation speed. They show the effect of increasing a parameter on the pump-specific characteristics head and efficiency for *BEP*. The results all apply to testing with clear water, i.e., no clogging behavior is considered.

**Table 3.** Geometric changes to the impeller and their effects on the pump-specific characteristics.

Geometric Change by Increasing the Parameter		Effects on the Pump-Specific Characteristics	
Parameter	Prefix	$H_{BEP}/\psi_{BEP}$	$\eta_{BEP}$
Impeller width	$b_2 \uparrow$	$\uparrow$	$\uparrow$
Impeller diameter	$D_2 \uparrow$	$\uparrow$	$\uparrow$
Blade number	$z \uparrow$	$\uparrow$	$\uparrow$
Blade outlet angle	$\beta_2 \uparrow$	$\uparrow$	$\uparrow$
Blade inlet angle	$\beta_1 \uparrow$	$\downarrow$	$\downarrow$
Blade thickness	$t \uparrow$	$\downarrow$	$\downarrow$
Winglets	$\uparrow$	$\uparrow$	$\uparrow$

**Table 4.** Geometric changes to the casing and changes to rotation speed and their effects on the pump-specific characteristics.

Geometric Change by Increasing the Parameter		Effects on the Pump-Specific Characteristics	
Parameter	Prefix	$H_{BEP}/\psi_{BEP}$	$\eta_{BEP}$
Volute width	$b_4 \uparrow$	$\downarrow$	$\downarrow$
Covering	$s \uparrow$	$\uparrow$	$\uparrow$
Suction pipe diameter	$D_s \uparrow$	unambiguous	unambiguous
Pressure pipe diameter	$D_d \uparrow$	$\downarrow$	$\rightarrow$
Geometry of suction pipe inlet	Straight	best	best
Geometry of casing	Ring	best	best
Rotation speed	$n \uparrow$	$\uparrow$	$\rightarrow$

Tables 3 and 4 summarize that increasing the impeller width, the impeller diameter, the blade number and the blade outlet angle all led to an increase of head, pressure coefficient and efficiency. However, increasing the blade inlet angle or the blade thickness resulted in a decrease of the head, pressure coefficient and efficiency. Adding winglets to the blade tips of an impeller was preferable in terms of increasing the head and efficiency compared to an impeller without winglets. Increasing the volute width led presumably to a decrease of head, pressure coefficient and efficiency. Increasing the covering presumably increase the head and efficiency, which means that the impeller should not be covered. The influence of suction pipe diameter was unambiguous, as some studies showed that an increase of suction pipe diameter led to an increase of head, pressure coefficient and efficiency, but some trends of studies showed the opposite. An increase of pressure pipe diameter led to a decrease of head. A straight design of the suction pipe inlet geometry was best in terms of head and efficiency compared to a design with a constriction and a design with a large radius of curvature. Similar, a ring casing design was best in terms of head and efficiency compared to a spiral casing and a half spiral casing. An increase of rotation speed led to an increase of head, while it had little effect on the efficiency.

## 5.2. Design Recommendations for Vortex Pumps

The single-parameter nature of the primary studies allows drawing causal inferences about the effect of geometric changes on the pump characteristics. Therefore, recommendations for the design of vortex pumps can be given if relations were unambiguous. We consider relations as unambiguous if multiple primary studies suggest similar trends between the parameter and the head or efficiency. Table 5 summarizes these design recommendations for the impeller, and Table 6 lists the design recommendations for the casing and for the rotation speed.

Finally, it remains to clarify which operating principle is more likely for a vortex pump. Based on the evaluation, the behavior is similar to a conventional centrifugal pump. A vortex pump responds to the change in the geometry sizes in trend with the same behavior as a conventional centrifugal pump.

For example, the coverage of the impeller should be avoided, and the influence of diameter change is similar. Standing out is only the parameter blade outlet angle, whereby this behavior is known by centrifugal pumps with semi-open impellers [37]. Therefore, it can be assumed that a vortex pump can be regarded as a centrifugal pump with a semi-open impeller and an enlarged side gap.

**Table 5.** Design recommendations for the impeller of a vortex pump.

Parameter	Prefix	Recommendation
Impeller width	$b_2$	↑
Impeller diameter	$D_2$	↑
Blade number	$z$	↑
Blade outlet angle	$\beta_2$	↑
Blade inlet angle	$\beta_1$	↓
Blade thickness	$t$	↓
Winglets	-	↑

**Table 6.** Design recommendations for the casing and rotational speeds of a vortex pump.

Parameter	Prefix	Recommendation
Volute width	$b_4$	↓
Covering	$s$	↑
Pressure pipe diameter	$D_d$	↓
Geometry of suction pipe inlet	-	Straight
Geometry of casing	-	Ring
Rotation speed	$n$	↑

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## Abbreviations

The following abbreviations are used in this manuscript:

<i>BEP</i>	Best Efficiency Point
$b_2$	impeller width
$b_4$	volute width
$D_2$	impeller diameter
$D_s$	suction pipe diameter
$D_d$	pressure pipe diameter
$g$	gravitational acceleration
$H$	head
$n$	rotation speed
$Q$	flow rate
$s$	covering
$t$	blade thickness
$z$	blade number
$\beta_1$	blade inlet angle
$\beta_2$	blade outlet angle
$\psi$	pressure coefficient
$\eta$	efficiency

## Appendix A

Table A1 summarizes the geometry data of the 53 primary investigations.

**Table A1.** Geometry data in the articles.

Source	Assessed Parameter	Design Type	D <sub>2</sub> (mm)	b <sub>2</sub> (mm)	z (-)	b <sub>4</sub> (mm)	β <sub>2</sub> (°)
<b>b<sub>2</sub>—Figure 9a,b</b>							
Rütschi [1]	b <sub>2</sub> = 15, 20, 25, 30 mm	covered	nn	15, 20, 25, 30	nn	nn	nn
Guan et al. [2]	b <sub>2</sub> = 30, 40, 50 mm	covered	182	30, 40, 50	nn	nn	nn
Wang [4]-a	b <sub>2</sub> = 30, 40, 50 mm	unknown	195	30, 40, 50	nn	nn	nn
Wang [4]-b	b <sub>2</sub> = 30, 40, 50 mm	unknown	180	30, 40, 50	nn	nn	nn
Zheng et al. [5]	b <sub>2</sub> = 14, 19, 22.5 mm	unknown	100	14, 19, 22.5	nn	40.5	nn
Sha et al. [6]	b <sub>2</sub> = 26, 28, 30 mm	covered	135	26, 28, 30	8	45	nn
Sha et al. [7]	b <sub>2</sub> = 35, 40 mm	covered	232	35, 40	10	100	nn
Sha et al. [8]	b <sub>2</sub> = 50, 55, 60, 65 mm	covered	286	50, 55, 60, 65	8	68	nn
Ohba et al. [9]	b <sub>2</sub> = 30, 40, 50, 60 mm	covered, pan impeller	265	30, 40, 50, 60	nn	100	nn
Masanori [10]	b <sub>2</sub> = 19.95, 40.5 mm	covered, pan impeller	300	19.95, 40.5	10	nn	90
<b>D<sub>2</sub>—Figures 10a,b and 11</b>							
Rütschi [1]	D <sub>2</sub> = 200, 210, 220, 230, 240, 250 mm	covered	200, 210, 220, 230, 240, 250	nn	nn	nn	nn
Guan et al. [2]	D <sub>2</sub> = 115, 125, 135, 140 mm	covered	115, 125, 135, 140	nn	nn	nn	nn
Wang [4]-c	D <sub>2</sub> = 170, 180, 195 mm	unknown	170, 180, 195	50	nn	nn	nn
Wang [4]-d	D <sub>2</sub> = 170, 180, 195 mm	unknown	170, 180, 195	30	nn	nn	nn
Zheng et al. [5]	D <sub>2</sub> = 90, 100, 118 mm	unknown	90, 100, 118	nn	nn	nn	nn
Sha et al. [6]	D <sub>2</sub> = 125, 135, 140 mm	covered	125, 135, 140	30	8	45	nn
Sha et al. [7]	D <sub>2</sub> = 125, 135, 140 mm	covered	125, 135, 140	26	7	40	nn
Sha et al. [8]	D <sub>2</sub> = 125, 135, 140 mm	unknown	125, 135, 140	32	8	45	nn
Ohba et al. [9]-a	D <sub>2</sub> = 195, 265 mm	covered	195, 265	25	nn	100	nn
Ohba et al. [9]-b	D <sub>2</sub> = 195, 265 mm	covered	195, 265	25	nn	50	nn
Lubieniecki [11]-a	D <sub>2</sub> = 381, 431.8, 457.2 mm	covered	381, 431.8, 457.2	76.2	nn	nn	90
Lubieniecki [11]-b	D <sub>2</sub> = 381, 431.8, 457.2 mm	covered	381, 431.8, 457.2	50.8	nn	nn	45
Lubieniecki [11]-c	D <sub>2</sub> = 381, 431.8, 457.2 mm	covered	381, 431.8, 457.2	38.1	nn	nn	45
<b>z—Figure 12a,b</b>							
Rütschi [1]	z = 6, 8, 9, 12	covered	nn	nn	6, 8, 9, 12	nn	nn
Guan et al. [2]	z = 6, 8, 10	covered	98	nn	6, 8, 10	nn	90
Masanori [10]	z = 6, 10	covered, pan impeller	300	40.05	6, 10	nn	90
<b>β<sub>2</sub>—Figure 13a,b</b>							
Guan et al. [2]	β <sub>2</sub> = 30°, 90°	covered	182	nn	7	nn	30, 90
Sha et al. [6]	β <sub>2</sub> = 45°, 90°, 135°	covered	105	30	8	45	45, 90, 135

Table A1. Cont.

Source	Assessed Parameter	Design Type	D <sub>2</sub> (mm)	b <sub>2</sub> (mm)	z (-)	b <sub>4</sub> (mm)	β <sub>2</sub> (°)
Sha et al. [8]	β <sub>2</sub> = 45°, 90°, 135°	covered	105	23	7	45	45, 90, 135
Masanori [10]	β <sub>2</sub> = 30°, 90°	covered, pan impeller	300	40.05	10	nn	30, 90
β <sub>1</sub> —Figure 14a							
Guan et al. [2]	β <sub>2</sub> = 30, 90°	covered	300	40.05	10	nn	30, 90
t—Figure 14b							
Guan et al. [2]	t / D <sub>2</sub> = 0.02, 0.05	covered	98	nn	nn	nn	nn
Winglets—Figure 15a							
Jiang et al. [12]	Depth of winglets	covered	nn	nn	nn	nn	nn
Front shroud—Figure 15b							
Zheng et al. [5]	With and without front shroud	unknown	nn	13	7	30.1	nn
Gerlach et al. [14]	With and without front shroud	open	230	nn	4	80	nn
b <sub>4</sub> —Figure 16a,b							
Zheng et al. [5]	b <sub>4</sub> = 25.5, 35.5, 44 mm	unknown	nn	nn	nn	25.5, 35.5, 44	nn
Sha et al. [6]	b <sub>4</sub> = 50, 56, 62 mm	covered	200	40	8	50, 56, 62	nn
Sha et al. [7]	b <sub>4</sub> = 80, 100, 125 mm	covered	268	50	8	80, 100, 125	nn
Sha et al. [8]	b <sub>4</sub> = 80, 100, 125 mm	covered	328	42	8	52, 60, 68	nn
Ohba et al. [9]	b <sub>4</sub> = 34, 50, 76 mm	covered, pan impeller	265	25	nn	34, 50, 76	nn
Covering—Figure 17a,b							
Rütschi [1]-a	s = 0, 20 mm	covered	nn	nn	6	nn	90
Rütschi [1]-b	s = 0, 20 mm	covered	nn	nn	12	nn	90
Sha and Hou [16]	s = 0, 3, 6, 8 mm	covered	94	20	8	25	90
D <sub>s</sub> —Figure 18a,b							
Guan et al. [2]	D <sub>s</sub> = 45, 55, 65 mm	covered	100	nn	nn	nn	nn
Zheng et al. [5]	D <sub>s</sub> = 49, 60 mm	unknown	93.4	22.5	8	40	nn
Sha et al. [6]	D <sub>s</sub> = 50, 55, 60, 65 mm	covered	105	30	8	45	nn
Ohba et al. [9]	D <sub>s</sub> = 53, 80, 104, 131 mm	covered, pan impeller	265	25	nn	50	nn
Geometry suction pipe—Figure 19b							
Rütschi [1]	Inlet straight, constriction, large radius	unknown	nn	nn	9	nn	90



Table A1. Cont.

Source	Assessed Parameter	Design Type	D <sub>2</sub> (mm)	b <sub>2</sub> (mm)	z (-)	b <sub>4</sub> (mm)	β <sub>2</sub> (°)
D <sub>d</sub> —Figure 20a							
Zheng et al. [5]	D <sub>d</sub> = 50, 80 mm	unknown	nn	nn	nn	nn	nn
Geometry casing— Figure 20b							
Zheng et al. [5]	Spiral, Ring, half Spiral	unknown	93.4	22.5	nn	nn	nn
n—Figure 21a,b							
Li and Feng [17]-a	n = 800, 1000, 1200 min <sup>-1</sup>	covered	150	45	6	50	90
Li and Feng [17]-b	n = 1000, 1200, 1300 min <sup>-1</sup>	covered	150	35	9	50	90
Sha and Bai [18]	n = 2200, 2400, 2600, 2800, 2850, 2900 min <sup>-1</sup>	unknown	96	22	8	25	90

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